



LEIDEN UNIVERSITY MEDICAL CENTER



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Capacity Planning and Scheduling for Semi-Urgent Surgeries at a Neurosurgery Department

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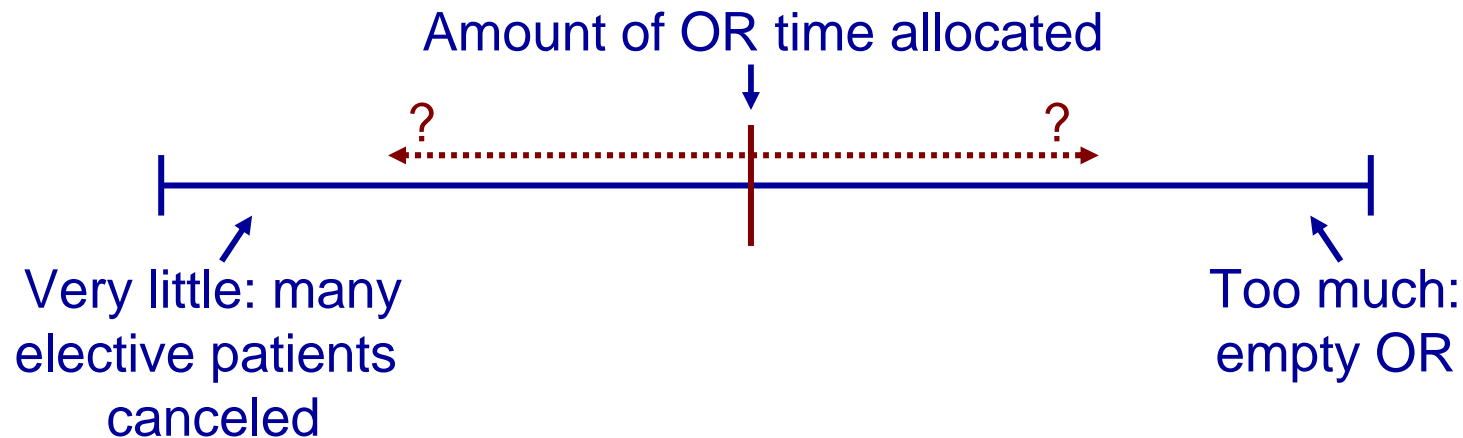
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Background

- Surgical department
- Three surgery types:
 - Elective
 - Urgent
 - Semi-urgent
- Urgent: within 24 hours
- Semi-urgent: within one or two weeks
- Consider only regular opening hours of OR complex

Motivation

- (Semi-)Urgent surgeries pose an uncertain demand on resources
- Urgent surgeries usually performed in overtime or at separate OR
→ do not take into account here
- Semi-urgent surgeries may not be performed in overtime
→ allocate part of regular OR time to semi-urgent surgeries



- Focus research on capacity allocation and planning for semi-urgent surgeries

Case - Introduction

- Case to illustrate modeling approach
- Neurosurgery department
- 8 OR sessions per week
- 40% of all incoming surgeries is classified semi-urgent

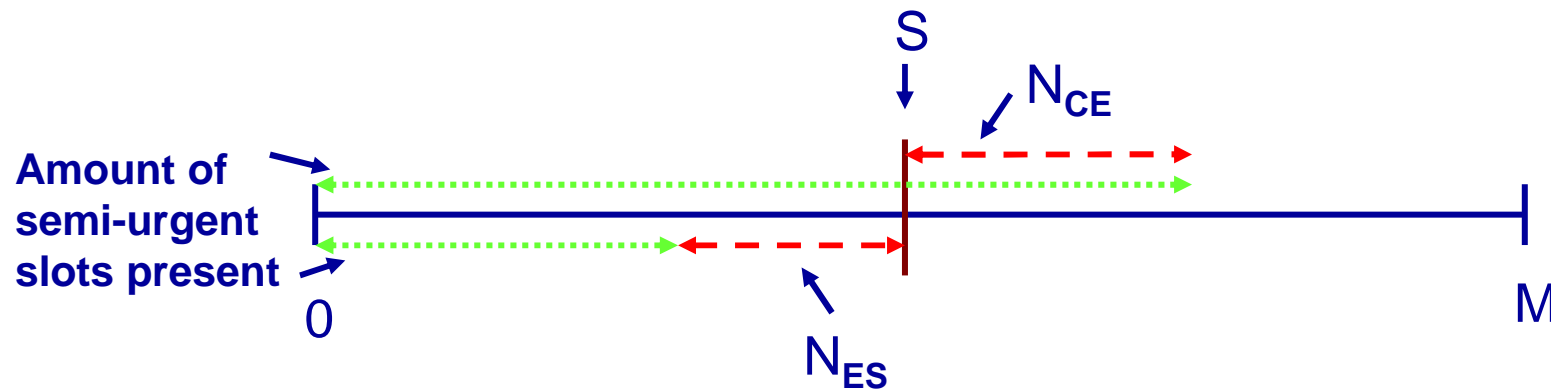
- Question 1: how much OR time should the neurosurgery department allocate to semi-urgent surgeries?

OR Capacity Planning (I)

- Slotted approach
- Each OR session has a duration of 3 slots
- Expected surgery duration is either 1, 2, or 3 slots
- Total # of slots available (M) = # of OR sessions \times 3
- Allocate fraction (S) of M to semi-urgent slots

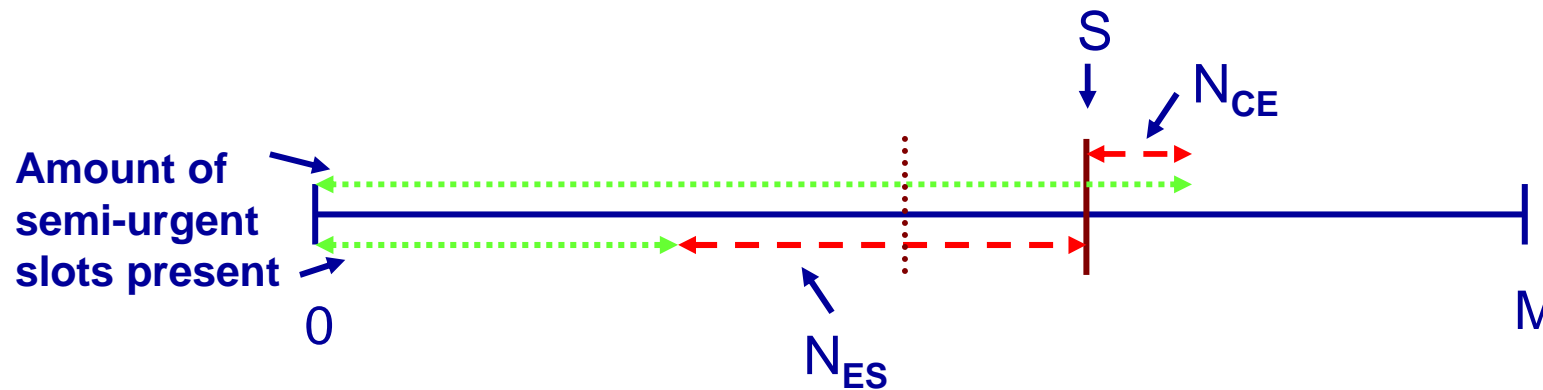
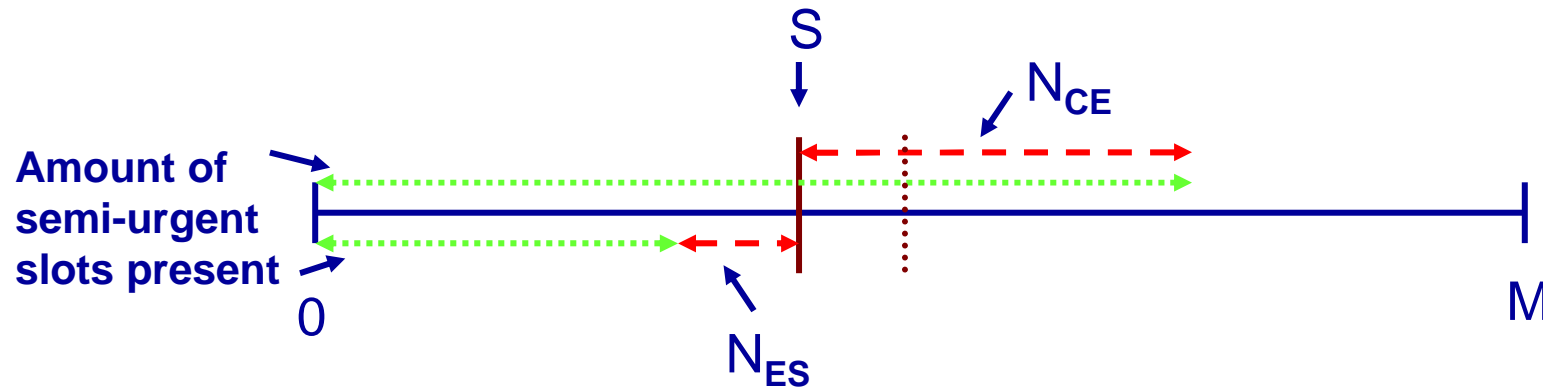
OR Capacity Planning (II)

- Note that
 - # of canceled elective slots (N_{CE}) depends on S
 - # of empty OR slots (N_{ES}) depends on S

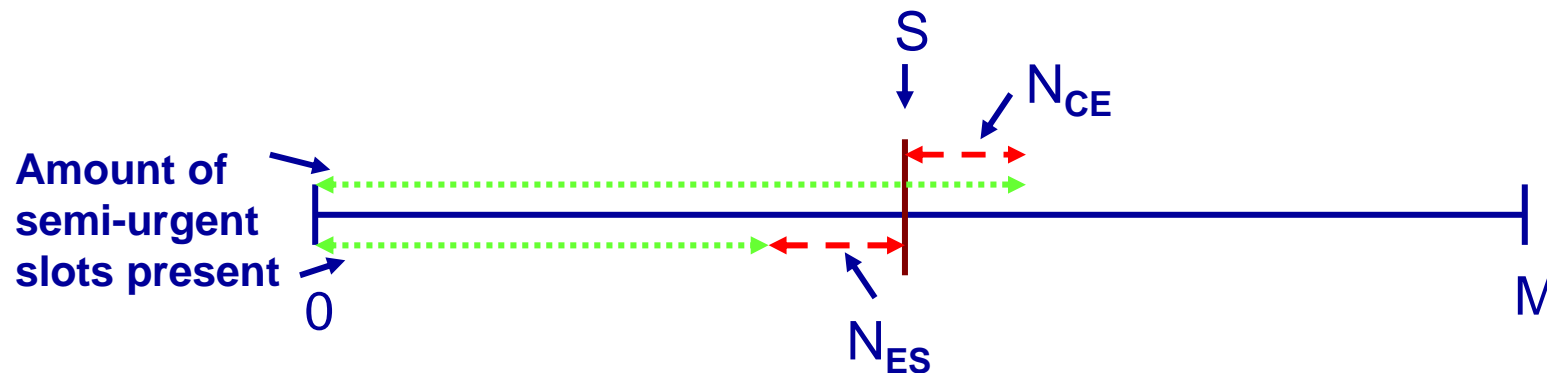


OR Capacity Planning (III)

- Note that
 - # of canceled elective slots (N_{CE}) depends on S
 - # of empty OR slots (N_{ES}) depends on S



OR Capacity Planning (IV)



- Use slotted queuing model to determine $E[N_{CE}]$ and $E[N_{ES}]$ for each S
- Assign cost C_{CE} to 1 canceled elective slot
- Assign cost C_{ES} to 1 empty OR slot

OR Capacity Planning (V)

- Find S^* that minimizes Expected Total Cost:

$$E[C_T] = E[N_{CE}] * C_{CE} + E[N_{ES}] * C_{ES}$$

- S^* is the optimal number of slots to allocate to semi-urgent surgeries, *given* C_{CE} and C_{ES}

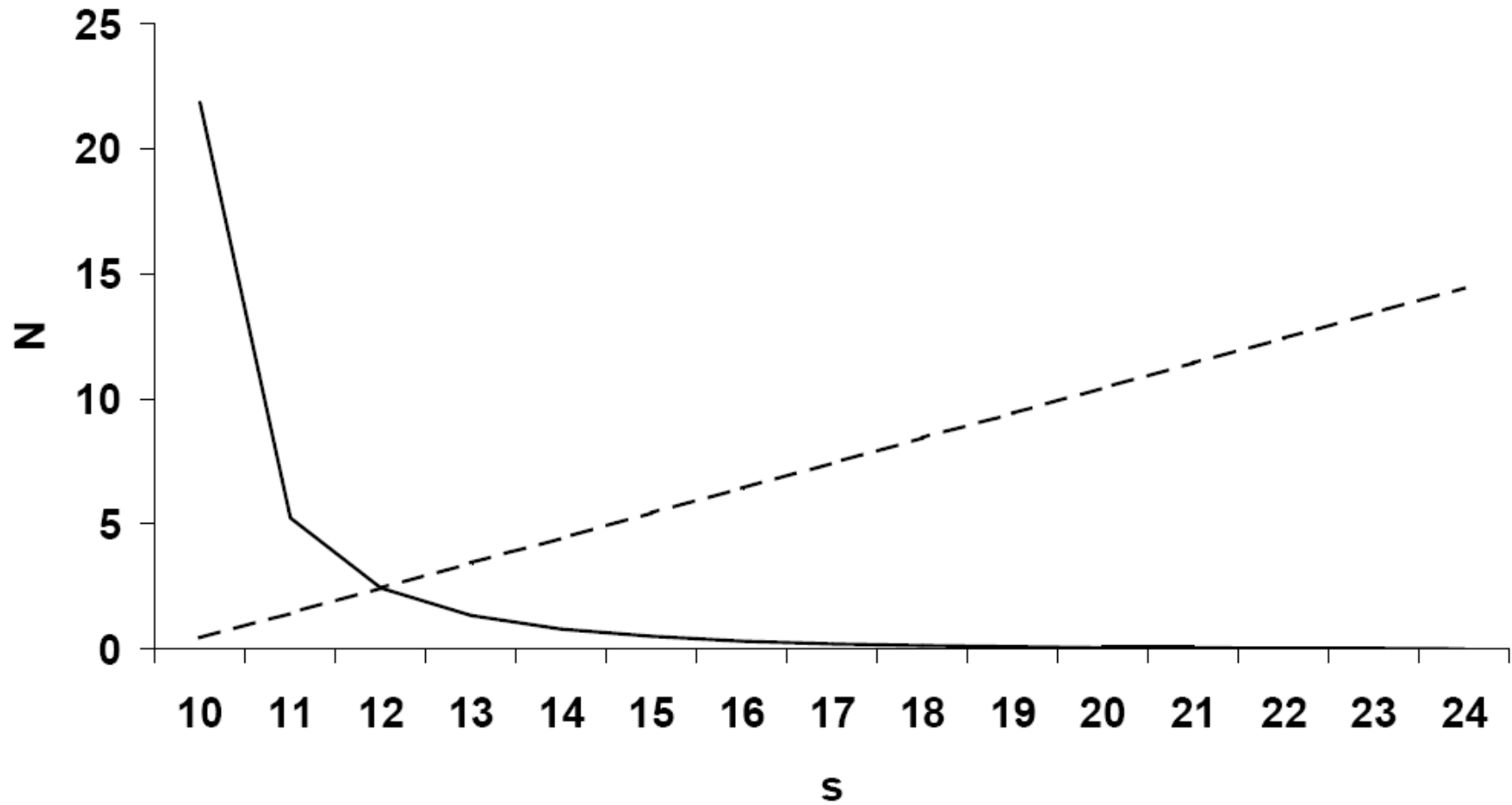
Case – Capacity Planning (I)

- Total # of slots available (M) = $8 \times 3 = 24$
- On average 5.5 semi-urgent surgeries arrive each week

- $P(1 \text{ slot surgery}) = 53\%$
- $P(2 \text{ slot surgery}) = 20\%$
- $P(3 \text{ slot surgery}) = 27\%$

- $S_{\min} = \text{expected \# of semi-urgent slot arrivals} = 9.6 \text{ slots}$
→ at least 10 slots required for stability

Case – Capacity Planning (II)

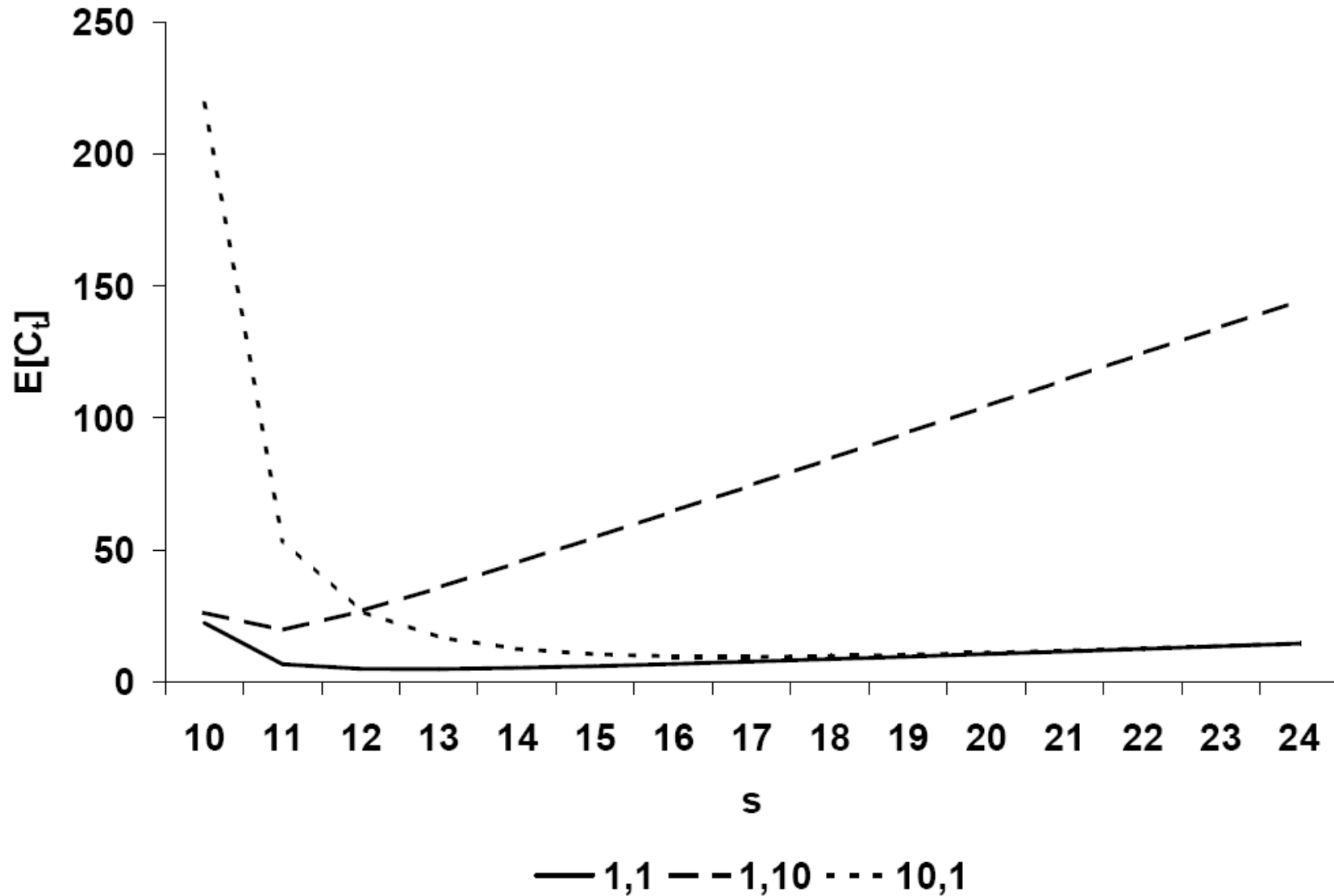


— Number of canceled elective slots
 - - Number of empty semi-urgent slots

Case – Capacity Planning (III)

- Note that value of optimal S^* depends on choice for C_{CE} and C_{ES}
- For CC_1 : $C_{CE} = 1$, $C_{ES} = 1$
→ $S^* = 13$
- For CC_2 : $C_{CE} = 1$, $C_{ES} = 10$
→ $S^* = 11$
- For CC_3 : $C_{CE} = 10$, $C_{ES} = 1$
→ $S^* = 17$
- Note that $S^* > S_{\min}$ in all cases!

Case – Capacity Planning (IV)

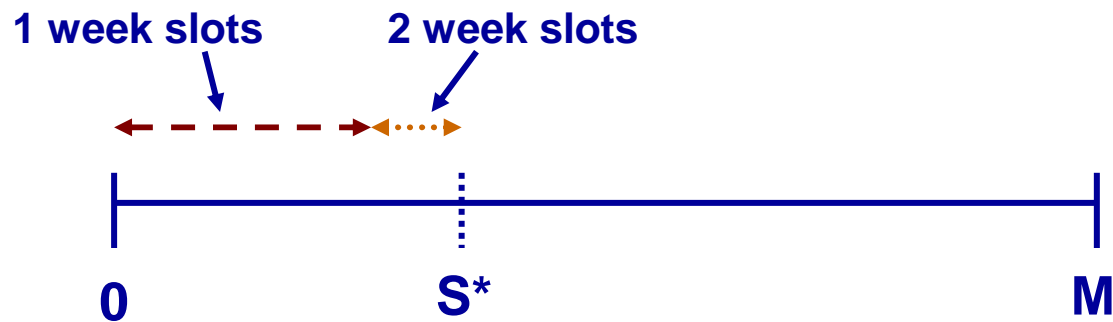


OR Scheduling (I)

- We now have determined the amount of OR time to dedicate to semi-urgent surgeries (S^*)
- Two types of semi-urgent surgeries:
 - within one week
 - within two weeks
- Schedule one week semi-urgent surgeries this week
- Two week semi-urgent surgeries can be postponed for one week
- Question 2: Now that we know S^* , when should we schedule two week semi-urgent surgeries?

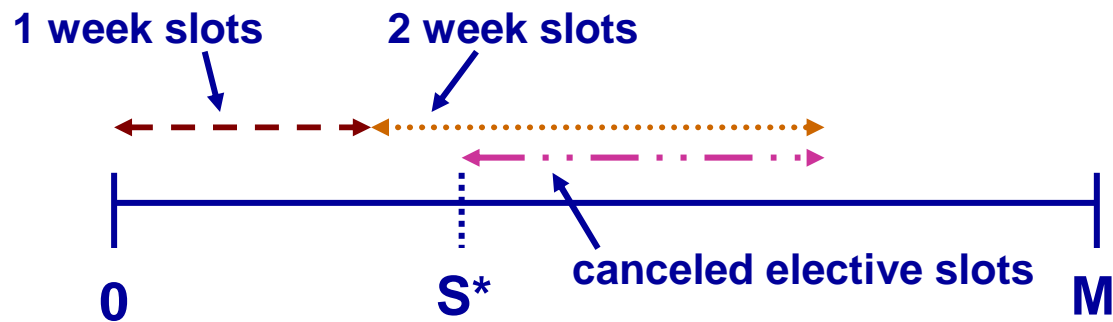
OR Scheduling (II)

- Question 2: Now that we know S^* , when should we schedule two week semi-urgent surgeries?
- Only up to S^* ?



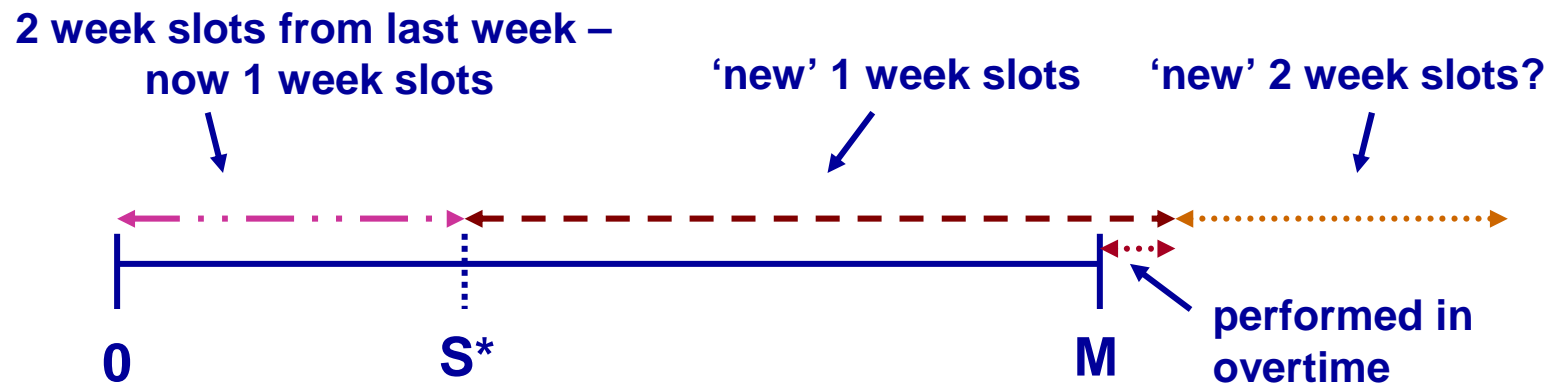
OR Scheduling (III)

- Question 2: Now that we know S^* , when should we schedule two week semi-urgent surgeries?
- Or more?
- Drawback: canceling of elective slots



OR Scheduling (IV)

- Question 2: Now that we know S^* , when should we schedule two week semi-urgent surgeries?
- Risk of postponement: 1 week surgeries in overtime



OR Scheduling (V)

- Develop Markov decision model
- Determine for each state (possible combination of one and two week slots present) an action (how many two week slots to plan this week)
- Use S^* calculated with queuing model
- Introduce additional costs for overflow of semi-urgent slots
- Minimize expected total discounted costs

Case – OR Scheduling (I)

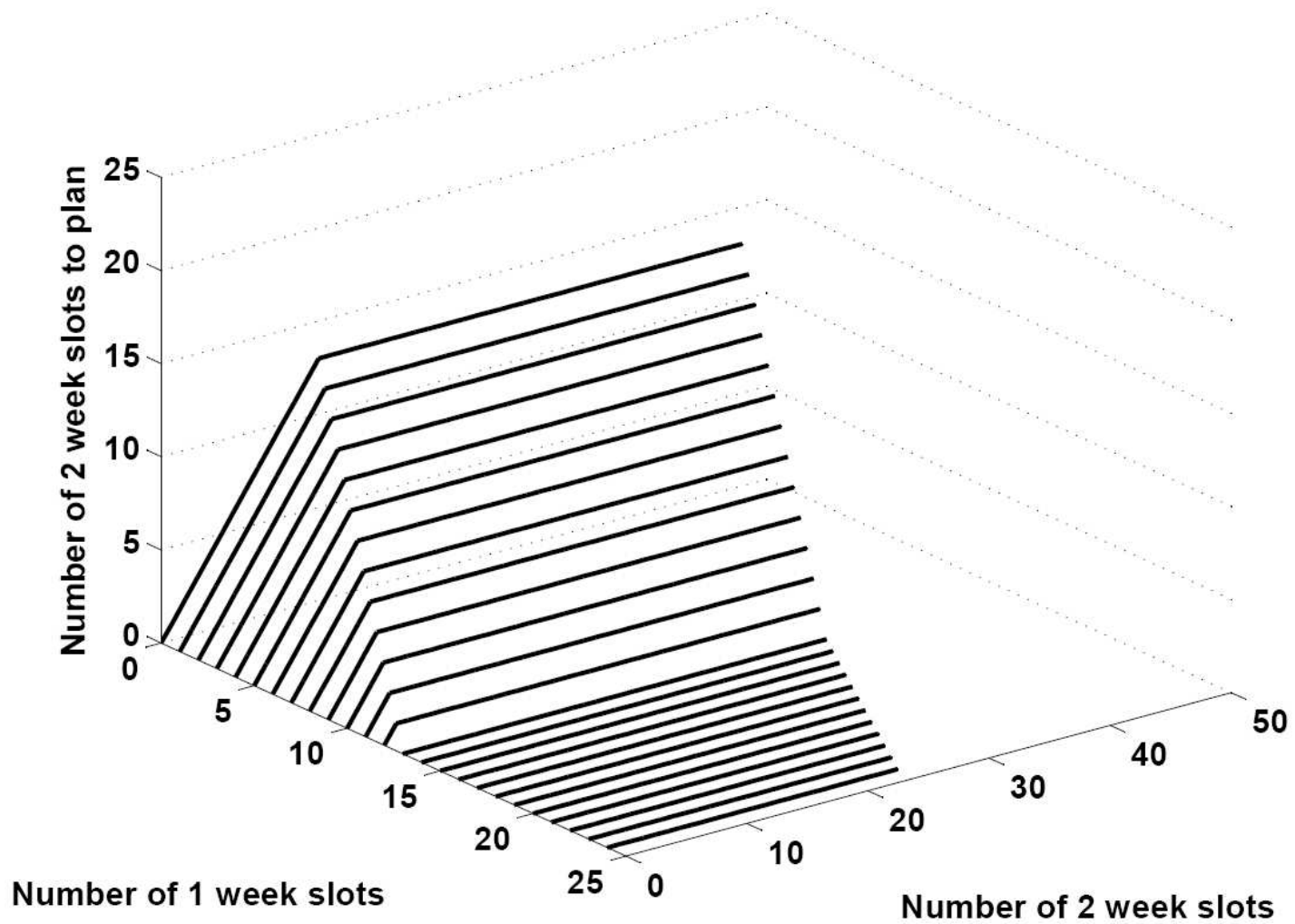
- Trivial problem?
- More than 1000 states for our case!
- Simplifies scheduling job

- Consider $S^* = 13$, $S^* = 11$, $S^* = 17$
(optimal S for CC_1 , CC_2 and CC_3)

- Graphic representation of strategies

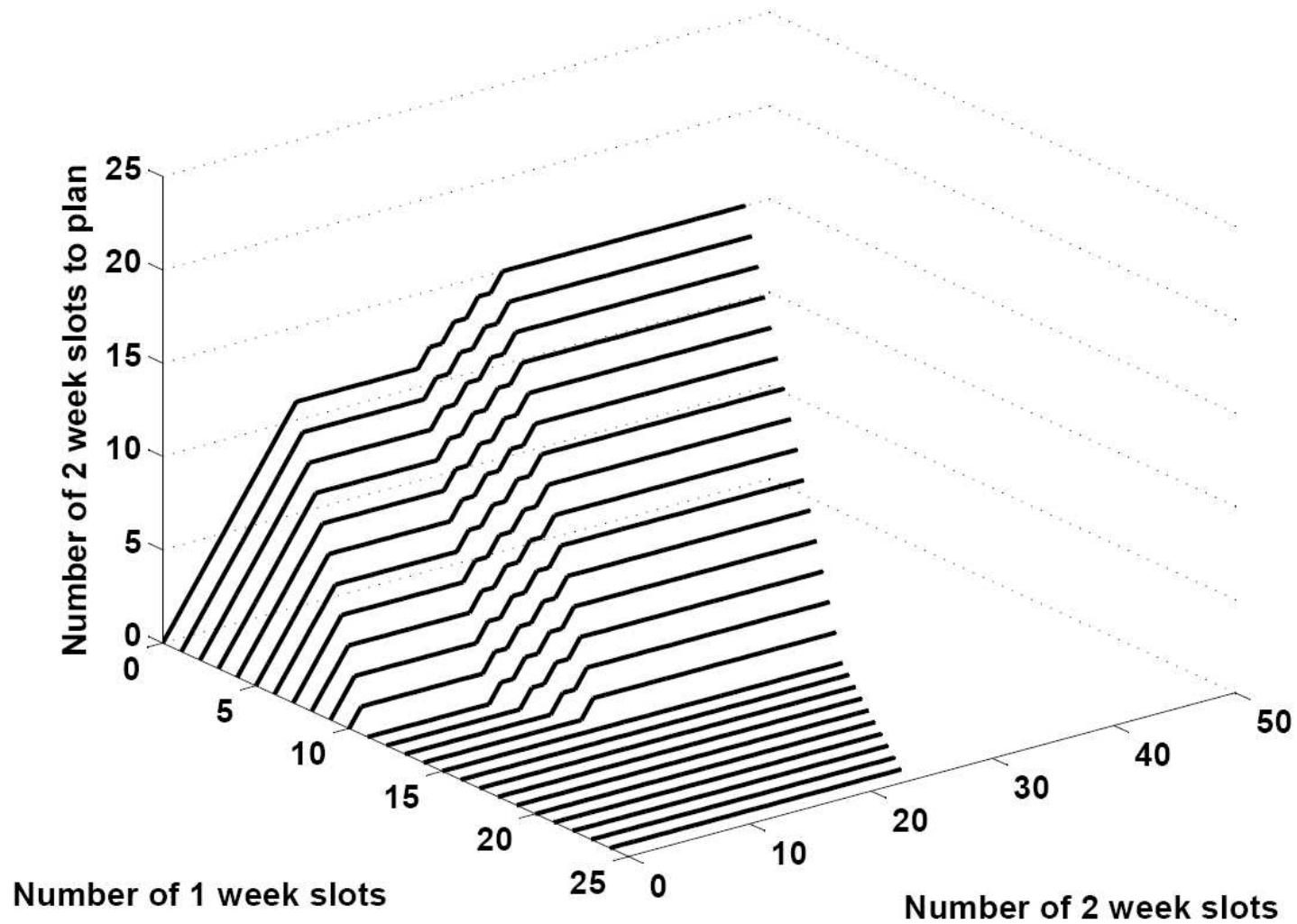
Case – OR Scheduling (II)

- $S^* = 13$



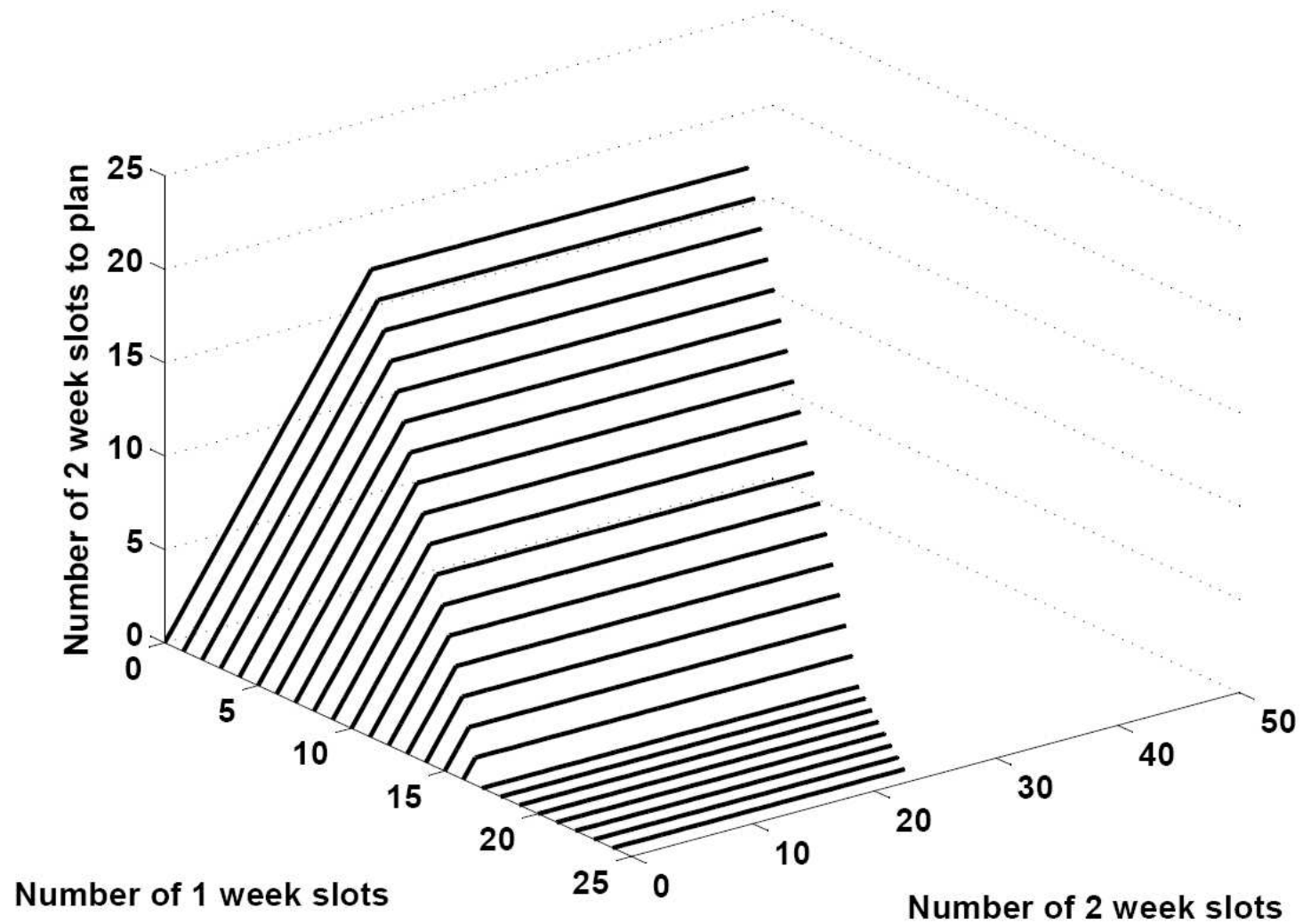
Case – OR Scheduling (III)

- $S^* = 11$



Case – OR Scheduling (IV)

- $S^* = 17$



Conclusion

- Use queuing model to determine amount of OR time to allocate to semi-urgent surgeries
→ dangerous to focus only on average behavior
- Use Markov decision model to decide upon actual scheduling
→ simplifies scheduling job
- Mathematical modeling approach allows for numerical comparison of alternative solutions



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Questions?